3	encoding a plaintext message word M to a ciphertext word C, wherein M corresponds to		
4	a number representative of a message and wherein		
5	$0 \le M \le n-1,$		
6	wherein n is a composite number formed by the product of $p_1 \cdot p_2 \cdot \cdot p_k$, k is an integer		
7	greater than 2 and $p_1, p_2,, p_k$ are distinct random prime numbers, C is a number		
8	representative of an encoded form of message word M, and wherein said encoding step		
9	comprises transforming said message word M to said ciphertext word C, whereby		
10	$C \equiv M^e \pmod{n}$,		
11	and wherein e is a number relatively prime to (p_1-1) , (p_2-1) ,, and (p_k-1) ; and		
12	decoding said ciphertext word C to a receive message word M', said decoding step being		
13	performed using a decryption exponent d that is defined by		
14	$d \equiv e^{-1} \mod ((p_1-1) (p_2-1) \dots (p_k-1)),$		
15	said decoding step including the further steps of,		
16	defining a plurality of k sub-tasks in accordance with		
17	$M_1' \equiv C_1^{d_1} \pmod{p_1},$		
18	$M_2' \equiv C_2^{d_2} \pmod{p_2},$		
19			
20	$M_k' \equiv C_k^{d_k} \pmod{p_k},$		
21	wherein		
22	$C_1 \equiv C \pmod{p_1},$		
23	$C_2 \equiv C \pmod{p_2},$		
24			
25	$C_k \equiv C \pmod{p_k},$		
26			
27	$d_1 \equiv d \pmod{(p_1 - 1)},$		
28	$d_2 \equiv d \pmod{(p_2 - 1)}$, and		
29	:		
30	$d_k \equiv d \pmod{(p_k - 1)},$		
31	solving said sub-tasks to determine results M ₁ ', M ₂ ', M _k ', and		

32	combining said results of said sub-tasks to produce said receive message word			
33	M', wherein M'=M.			
1	22. (Three Times Amended) A cyptographic communications system for establishing			
2	communications, comprising:			
3	a communication medium;			
4	encoding means coupled to said communication medium and adapted for transforming a			
. ,5	transmit message word M to a ciphertext word C and for transmitting said ciphertext word C on			
6	said medium, wherein M corresponds to a number representative of a message, and			
7	$0 \le M \le n-1$, wherein n is a composite number of the form,			
8	$\mathbf{n} = \mathbf{p}_1 \cdot \mathbf{p}_2 \cdot \ldots \cdot \mathbf{p}_k$			
9	wherein k is an integer greater than 2 and $p_1, p_2,, p_k$ are distinct random prime			
10	numbers, and wherein said ciphertext word C corresponds to a number representative of an			
11	enciphered form of said message word M and corresponds to			
12	$C \equiv M^e \pmod{n}$			
13	wherein e is a number relatively prime to (p_1-1) , (p_2-1) ,, and (p_k-1) ; and			
14	decoding means communicatively coupled with said communication medium for			
15	receiving said ciphertext word C via said medium, said decoding means being operative to			
16	perform a decryption process for transforming said ciphertext word C to a receive message word			
17	M', wherein M' corresponds to a number representative of a deciphered form of C, said			
18	decryption process using a decryption exponent d that is defined by			
. 19	$d \equiv e^{-1} \mod ((p_1-1) (p_2-1) \dots (p_k-1)),$			
20	said decryption process including the steps of			
21	defining a plurality of k sub-tasks in accordance with			
22	$M_1' \equiv C_1^{d_1} \pmod{p_1},$			
23	$M_2' \equiv C_2^{d_2} \pmod{p_2},$			
24				
25	$M_k' \equiv C_k^{d_k} \pmod{p_k},$			
26	wherein			

```
C_1 \equiv C \pmod{p_1},
27
                                       \dot{C}_2 \equiv C \pmod{p_2},
28
29
                                       C_k \equiv C \pmod{p_k},
30
31
                                       d_1 \equiv d \pmod{(p_1 - 1)},
32
                                       d_2 \equiv d \pmod{(p_2 - 1)},
33
34
                                       d_k \equiv d \pmod{(p_k - 1)},
35
                       solving said sub-tasks to determine results M1', M2', ... Mk', and
36
                       combining said results of said sub-tasks to produce said receive message word M'
37
               whereby M'=M.
38
               (Three Times Amended) A method for establishing cryptographic communications,
       27.
  1
       comprising the step of:
  2
               encoding a plaintext message word M to a ciphertext word C, wherein M corresponds to
  3
        a number representative of a message, and
  4
                0 \le M \le n-1,
  5
       n being a composite number formed from the product of p<sub>1</sub>•p<sub>2</sub>•...•p<sub>k</sub>, wherein k is an integer
  6
       greater than 2 and p_1, p_2, ..., p_k are distinct random prime numbers, and wherein the ciphertext
  7
       word C is a number representative of an encoded form of message word M, wherein said step of
  8
        encoding includes the steps of
  9
                defining a plurality of k sub-tasks in accordance with
 10
                                C_1 \equiv M_1^{e_1} \pmod{p_1},
 11
                                C_2 \equiv M_2^{e_2} \pmod{p_2},
 12
 13
                                C_k \equiv M_k^{e_k} \pmod{p_k},
 14
                         where
 15
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Applicant: COLLINS et al Serial No: 09/328,726

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M_1 \equiv M \pmod{p_1},
16
17
                              M_2 \equiv M \pmod{p_2},
18
                              M_k \equiv M \pmod{p_k},
19
20
                              e_1 \equiv e \pmod{(p_1 - 1)}
21
22
                              e_2 \equiv e \pmod{(p_2 - 1)}, and
23
                              e_k \equiv e \pmod{(p_k - 1)}
24
                       wherein e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1),
25
               solving said sub-tasks to determine results C<sub>1</sub>, C<sub>2</sub>, ... C<sub>k</sub>, and
26
               combining said results of said sub-tasks to produce said ciphertext word C.
27
               (Three Times Amended) A cyptographic communications system for establishing
 1
       32.
 2
       communications, comprising:
 3
               a communication medium;
               encoding means coupled to said communication medium and operative to transform a
 4
       transmit message word M to a ciphertext word C, and to transmit said ciphertext word C on said
 5
       medium, wherein M corresponds to a number representative of a message, and
 6
 7
               0 \le M \le n-1,
       n being a composite number formed from the product of p_1 \cdot p_2 \cdot \ldots \cdot p_k wherein k is an integer
 8
       greater than 2 and p_1, p_2, ..., p_k, are distinct random prime numbers, and wherein the ciphertext
 9
       word C is a number representative of an encoded form of message word M, said encoding means
10
       being operative to transform said transmit message word M to said ciphertext word C by
11
       performing an encoding process comprising the steps of
12
               defining a plurality of k sub-tasks in accordance with
13
                               C_1 \equiv M_1^{e_1} \pmod{p_1},
14
                               C_2 \equiv M_2^{e_2} \pmod{p_2},
15
16
```

```
C_k \equiv M_k^{e_k} \pmod{p_k},
17
18
                       where
 19
                               M_1 \equiv M \pmod{p_1},
 20
                               M_2 \equiv M \pmod{p_2},
 21
                                M_k \equiv M \pmod{p_k},
 22
 23
 24
                                e_1 \equiv e \pmod{(p_1 - 1)}
                                e_2 \equiv e \pmod{(p_2 - 1)}, and
 25
 26
 27
                                e_k \equiv e \pmod{(p_k - 1)},
                        wherein e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1),
 28
                solving said sub-tasks to determine results C<sub>1</sub>, C<sub>2</sub>,... C<sub>k</sub>, and
. 29
                combining said results of said sub-tasks to produce said ciphertext word C.
 30
        37. (Three Times Amended) A method for establishing cryptographic communications,
  1
        comprising the steps of:
  2
                decoding a ciphertext word C to a message word M, wherein M corresponds to a number
  3.
        representative of a message and wherein
  4
                0 \le M \le n-1
   5
        wherein n is a composite number formed by the product of p_1 \cdot p_2 \cdot ... \cdot p_k, k is an integer greater
   6
        than 2 and p_1, p_2, ..., p_k are distinct random prime numbers, C is a number representative of an
   7
        encoded form of message word M that is encoded by transforming said message word M to said
   8
        ciphertext word C whereby
  9
                C \equiv M^e \pmod{n},
 10
                and wherein e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1);
 11
                said decoding step being performed using a decryption exponent d that is defined by
 12
                         d \equiv e^{-1} \mod ((p_1-1) (p_2-1) \dots (p_k-1)),
 13
```

```
wherein said step of decoding includes the steps of
14
                     defining a plurality of k sub-tasks in accordance with
15
                             M_1 \equiv C_1^{d_1} \pmod{p_1},
16
                             M_2 \equiv C_2^{d_2} \pmod{p_2},
17
18
                              M_k \equiv C_k^{d_k} \pmod{p_k},
19
                      wherein
20
                              C_1 \equiv C \pmod{p_1},
21
                              C_2 \equiv C \pmod{p_2},
22
23
                              C_k \equiv C \pmod{p_k},
24
25
                               d_1 \equiv d \pmod{(p_1 - 1)},
26
                               d_2 \equiv d \pmod{(p_2 - 1)}, and
27
 28
                               d_k \equiv d \pmod{(p_k - 1)},
 29
                       solving said sub-tasks to determine results M_1, M_2, ... M_k, and
 30
                       combining said results of said sub-tasks to produce said message word M.
 31
       42. (Three Times Amended) A cyptographic communications system for establishing
  1
        communications, comprising:
  2
                a communication medium;
  3
                decoding means communicatively coupled with said communication medium for
   4
        receiving a ciphertext word C via said medium, and being operative to transform said ciphertext
   5
        word C to a receive message word M', wherein a message M corresponds to a number
   6
        representative of a message and wherein,
   7
                0 \le M \le n-1
   8
```

```
9
       wherein n is a composite number formed by the product of p<sub>1</sub>•p<sub>2</sub>•...•p<sub>k</sub>, k is an integer greater
       than 2 and p_1, p_2, ..., p_k are distinct random prime numbers, and wherein said ciphertext word C
10
       is a number representative of an encoded form of said message word M that is encoded by
11
12
       transforming M to said ciphertext word C whereby,
               C \equiv M^e \pmod{n},
13
               and wherein e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1);
14
               said decoding means being operative to perform a decryption process using a decryption
15
       exponent d that is defined by
16
                        d \equiv e^{-1} \mod ((p_1-1) (p_2-1) \dots (p_k-1)),
17
               said decryption process including the steps of
18
                        defining a plurality of k sub-tasks in accordance with,
19
                                M_1' \equiv C_1^{d_1} \pmod{p_1}
20
                                M_2' \equiv C_2^{d_2} \pmod{p_2},
21
22
                                M_k' \equiv C_k^{d_k} \pmod{p_k}
23
                        wherein.
24
                                 C_1 \equiv C \pmod{p_1},
25
                                 C_2 \equiv C \pmod{p_2},
26
27
                                 C_k \equiv C \pmod{p_k},
28
29
                                 d_1 \equiv d \pmod{(p_1 - 1)},
30
                                 d_2 \equiv d \pmod{(p_2 - 1)}, and
31
32
                                 d_k \equiv d \pmod{(p_k - 1)}
33
                        solving said sub-tasks to determine results M<sub>1</sub>', M<sub>2</sub>', ... M<sub>k</sub>', and
34
                         combining said results of said sub-tasks to produce said receive message word
35
36
                M', whereby M'=M.
```

```
(Three Times Amended) A method for generating a digital signature, comprising the step
      47.
1
      of:
2
               signing a plaintext message word M to create a signed ciphertext word C, wherein M
 3
      corresponds to a number representative of a message, and
 5
               0 \le M \le n-1,
      n being a composite number formed from the product of p<sub>1</sub>•p<sub>2</sub>•...•p<sub>k</sub>, wherein k is an integer
 6
      greater than 2 and p_1, p_2, ..., p_k are distinct random prime numbers, and wherein the signed
 7
       ciphertext word C is a number representative of a signed form of message word M, wherein
 8
               C \equiv M^d \pmod{n}, and
 9
               wherein said step of signing includes the steps of
10
               defining a plurality of k sub-tasks in accordance with
11
                                C_1 \equiv M_1^{d_1} \pmod{p_1},
12
                                C_2 \equiv M_2^{d_2} \pmod{p_2},
13
14
                                C_k \equiv M_k^{d_k} \pmod{p_k}
15
16
                        where
17
                                 M_1 \equiv M \pmod{p_1},
18
                                 M_2 \equiv M \pmod{p_2}
19
                                 M_k \equiv M \pmod{p_k},
20
21
                                 d_1 \equiv d \pmod{(p_1 - 1)},
22
                                 d_2 \equiv d \pmod{(p_2 - 1)}, and
23
24
                                 d_k \equiv d \pmod{(p_k - 1)},
25
26
                        wherein d is defined by
                                 d = e^{-1} \mod ((p_1 - 1) \cdot (p_2 - 1) \cdot ... \cdot (p_k - 1)), and
27
                                 e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1),
28
```

29	•	solving said sub-tasks to determine results C ₁ , C ₂ , C _k , and			
30		combining said results of said sub-tasks to produce said ciphertext word C.			
1	52.	(Three Times Amended) A digital signature generation system, comprising:			
2		a communication medium;			
3 .		digital signature generating means coupled to said communication medium and operative			
4	to trai	nsform a transmit message word M to a signed ciphertext word C, and to transmit said			
5		d ciphertext word C on said medium, wherein M corresponds to a number representative of			
6	a mes	sage, and			
7		$0 \le M \le n-1,$			
8	n being a composite number formed from the product of p ₁ •p ₂ ••p _k wherein k is an integer				
9	greater than 2 and $p_1, p_2,, p_k$, are distinct random prime numbers, and wherein the signed				
10	ciphe	rtext word C is a number representative of a signed form of said message word M, wherein			
11		$C \equiv M^d \pmod{n},$			
12		said digital signature generating means being operative to transform said transmit			
13	mess	age word M to said signed ciphertext word C by performing a digital signature generating			
14	proce	ess comprising the steps of,			
15		defining a plurality of k sub-tasks in accordance with,			
16		$C_1 \equiv M_1^{d_1} \pmod{p_1},$			
17		$C_2 \equiv M_2^{d_2} \pmod{p_2},$			
18					
19		$C_k \equiv M_k^{d_k} \pmod{p_k},$			
20		where,			
21		$\mathbf{M}_1 \equiv \mathbf{M} \; (\bmod \; \mathbf{p}_1),$			
22		$M_2 \equiv M \pmod{p_2},$			
23		:			
24		$M_k \equiv M \pmod{p_k}$			
25					

26

 $d_1 \equiv d \pmod{(p_1 - 1)},$

```
d_2 \equiv d \pmod{(p_2 - 1)}, and
27
28
                                d_k \equiv d \pmod{(p_k - 1)},
29
                        wherein d is defined by,
30
                                d = e^{-1} \mod ((p_1 - 1) \cdot (p_2 - 1) \cdot ... \cdot (p_k - 1)), and
31
                                e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1),
32
               solving said sub-tasks to determine results C1, C2, ... Ck, and
33
                combining said results of said sub-tasks to produce said signed ciphertext word C.
34
               (Three Times Amended) A digital signature process, comprising the steps of:
  1
       57.
                signing a plaintext message word M to create a signed ciphertext word C, wherein M
  2
       corresponds to a number representative of a message and wherein
  3
                        0 \le M \le n-1
  4
                wherein n is a composite number formed by the product of p<sub>1</sub>•p<sub>2</sub>•...•p<sub>k</sub>, k is an integer
  5
                greater than 2 and p_1, p_2, ..., p_k are distinct random prime numbers, C is a number
  6
                representative of a signed form of message word M, and wherein said encoding step
  7
                comprises transforming said message word M to said ciphertext word C whereby,
  8
                        C \equiv M^d \pmod{n},
  9
                         wherein d is defined by
 10
                                 d \equiv e^{-1} \mod ((p_1 - 1) \cdot (p_2 - 1) \cdot \dots \cdot (p_k - 1)), and
 11
                                 e is a number relatively prime to (p<sub>1</sub>-1), (p<sub>2</sub>-1), ..., and (p<sub>k</sub>-1); and
 12
                verifying said ciphertext word C to a receive message word M' by performing the steps
 13
 14
        of,
                         defining a plurality of k sub-tasks in accordance with
 15
                                         M_1' \equiv C_1^{e_1} \pmod{p_1},
 16
                                          M_2' \equiv C_2^{e_2} \pmod{p_2},
 17
 18
                                          M_k' \equiv C_k^{e_k} \pmod{p_k},
 19
                                  wherein
 20
```

```
C_1 \equiv C \pmod{p_1},
21
                                        C_2 \equiv C \pmod{p_2}
22
23
                                        C_k \equiv C \pmod{p_k},
24
25
                                        e_1 \equiv e \pmod{(p_1 - 1)}
26
                                        e_2 \equiv e \pmod{(p_2 - 1)}, and
27
28
                                         e_k \equiv e \pmod{(p_k - 1)}
29
                        solving said sub-tasks to determine results M<sub>1</sub>', M<sub>2</sub>', ... M<sub>k</sub>', and
30
                        combining said results of said sub-tasks to produce said receive message word
31
               M', whereby M'=M.
32
       62. (Three Times Amended) A digital signature system, comprising:
  1
  2
              a communication medium;
                digital signature generating means coupled to said communication medium and adapted
  3
        for transforming a message word M to a signed ciphertext word C and for transmitting said
  4
        signed ciphertext word C on said medium, wherein M corresponds to a number representative of
  5
  6
        a message, and
                0 \le M \le n-1, wherein n is a composite number of the form
  7
  8
                n = p_1 \cdot p_2 \cdot \ldots \cdot p_k
                wherein k is an integer greater than 2 and p<sub>1</sub>, p<sub>2</sub>, ...,p<sub>k</sub> are distinct random prime
  9
        numbers, and wherein said signed ciphertext word C corresponds to a number representative of a
 10
 11
        signed form of said message word M and corresponds to
                C \equiv M^d \pmod{n},
 12
                         wherein d is defined by
 13
                         d \equiv e^{-1} \mod ((p_1 - 1) \cdot (p_2 - 1) \cdot \dots \cdot (p_k - 1)), \text{ and}
 14
                         e is a number relatively prime to (p_1-1), (p_2-1), ..., and (p_k-1); and
 15
```

16	digital signature verification means communicatively coupled with said communication
17	medium for receiving said signed ciphertext word C via said medium, and being operative to
18	verify said signed ciphertext word C by performing the steps of,
19	defining a plurality of k sub-tasks in accordance with
20	$M_1' \equiv C_1^{e_1} \pmod{p_1},$
21	$\mathbf{M_2'} \equiv C_2^{e_2} \pmod{p_2},$
22	
23	$M_k' \equiv C_k^{e_k} \pmod{p_k},$
24	` wherein
25	$C_1 \equiv C \pmod{p_1},$
26	$C_2 \equiv C \pmod{p_2},$
27	
28	$C_k \equiv C \pmod{p_k}$
29	
30	$e_1 \equiv e \pmod{(p_1 - 1)},$
31	$e_2 \equiv e \pmod{(p_2 - 1)},$
32	
33	$e_k \equiv e \pmod{(p_k - 1)},$
34	solving said sub-tasks to determine results M_1 , M_2 , M_k , and
35	combining said results of said sub-tasks to produce said receive message word M'
36	wherein M'=M.